

Optimization of Hydrometallurgical Recovery of MnO₂ from Dry Cell Waste Using Response Surface Methodology

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Abstract

This study aims to recover manganese dioxide from depleted dry cell batteries using a hydrometallurgical process optimized by response surface methodology (RSM). The research is motivated by the high industrial demand for imported MnO₂ and environmental issues associated with hazardous spent battery waste. The recovery process involved microwave-assisted leaching using 1.2 M H₂SO₄ with the addition of H₂O₂ reductant (0–2% w/v), followed by oxidative precipitation using 0.25 M KMnO₄. Variables tested included reductant concentration and leaching time. Based on RSM optimization using the central composite design model, optimum conditions were achieved at an H₂O₂ concentration of 2% w/v and a leaching time of 39.15 min. Under these conditions, a recovery rate of 96.76% was obtained with a desirability value of 0.805 and a model *R*² of 0.9151. The final product exhibited Mn purity of 96.10–97.33%, a significant increase from the raw material (64.61%) and surpassing the commercial MnO₂ standard (>92%). This research highlights the synergistic integration of microwave-assisted heating and chemical reduction. While previous studies have applied these techniques independently, their combined effect drastically accelerates the extraction kinetics, reducing the leaching time to under 40 min, which is significantly faster than conventional methods while still achieving commercial-grade purity from complex secondary waste. This study demonstrates that microwave-assisted hydrometallurgy is a highly time-efficient and sustainable approach for recycling battery waste into high-value industrial raw materials, supporting sustainable development goals principles.

Keywords

dry cell, hydrometallurgy, leaching, manganese dioxide, RSM

1 Introduction

MnO₂ is an essential compound widely utilized across various industrial sectors. In filtration processes, MnO₂ is commonly employed as a filter medium due to its ability to adsorb iron (Fe) and manganese (Mn) ions present in wastewater [1]. In the steel industry, MnO₂ is used as a protective coating for iron-based soft magnetic composites (FeSMCs) to enhance material performance [2]. Furthermore, MnO₂ serves as an active component in lithium-ion batteries as well as zinc–manganese batteries [3]. According to data from Statistics Indonesia in 2025, Indonesia remains dependent on imports to meet domestic MnO₂ demand, with import volumes reaching

24,531,206 kg in last 2024, representing an increase of 32.32% compared to the previous year [4]. MnO₂ is classified as hazardous and toxic waste (B3) due to its potential environmental and health risks [5]. MnO₂ is an inorganic material that is soluble in acidic reagents [6, 7]. Structurally, α -MnO₂ consists of double chains of MnO₆ octahedra, whereas β -MnO₂ is composed of single-chain octahedral frameworks [8].

The maximum allowable concentration of manganese in water for hygiene and sanitation purposes, as stipulated by the Indonesian Minister of Health Regulation No. 2 year 2023, is 0.1 mg/L [9]. Exposure to MnO₂

concentrations exceeding this threshold may lead to ecotoxicological effects that pose risks to human health. MnO_2 can undergo bioaccumulation through water systems, potentially causing neurological disorders and damage to internal organs [10]. In response to these challenges, the government, through the sustainable development goals (SDGs) framework, promotes the recycling of hazardous waste to mitigate environmental pollution while simultaneously fulfilling industrial demand for strategic materials, including MnO_2 . A dry cell battery is a primary battery with a nominal voltage of 1.5 V, consisting of a zinc anode, a MnO_2 -carbon cathode, a carbon rod, and ammonium chloride electrolyte, in which electrical energy is generated through the reduction-oxidation process. Dry cell works through a reduction-oxidation reaction, one of which is the reaction between zinc oxide and NH_4Cl that converts ZnO into zinc chloride [11–14].

MnO_2 contained in spent dry cell batteries can be separated from impurities using pyro-metallurgical, biometallurgical, and hydrometallurgical processes. Pyrometallurgy relies on high-temperature energy input, which increases operational costs and poses environmental risks due to the generation of hazardous slag and residues requiring further treatment [15]. Biometallurgy employs microorganisms to leach metals from waste materials; however, this approach demands strict control of operating conditions such as temperature, pH and nutrient availability [16]. In contrast, hydrometallurgical processing is based on the selective dissolution of metals using acidic solvents and allows the separation of soluble components from insoluble impurities. Compared to other methods, hydrometallurgy is considered to be the most efficient and practical approach for MnO_2 recovery, as it operates at relatively low temperatures and does not require microbial management. This method involves metal dissolution in strong acid solutions, followed by purification steps to obtain MnO_2 with high purity and recovery efficiency [17, 18].

Hydrometallurgical processing involves the dissolution of metals in strong acidic solutions under controlled heating, followed by purification steps to obtain high-purity metal products [18–22]. Previous studies have demonstrated that microwave-assisted heating significantly enhances metal extraction efficiency [23, 24]. Lin et al. [25] reported a MnO_2 leaching yield of 95.07% using microwave heating, which was approximately 20% higher than that achieved with conventional heating when using 1.2 M H_2SO_4 and liquid to solid ratio 10 mL/g. Similarly, Chang et al. [26]

observed a MnO_2 leaching efficiency of 90% under microwave-assisted hydrometallurgical conditions from manganese ore. In addition to heating methods, the use of reducing agents can enhance metal extraction efficiency from metal ore [22, 27]. In other study, 0.8 M H_2O_2 has been shown to substantially improve MnO_2 leaching efficiency from manganese ore, reaching up to 99.04% under conventional hydrometallurgical conditions [28].

To determine optimal operating conditions, response surface methodology (RSM) is employed to evaluate the combined effects of multiple independent variables on the extraction response [29]. RSM integrates factorial techniques and ANOVA to model response variables, primarily through the application of either central composite design (CCD) or Box-Behnken design (BBD) [30–32]. Specifically, CCD utilizes five factor levels and axial points to achieve high precision in surface curvature estimation, whereas BBD operates on only three levels, offering greater experimental efficiency by excluding extreme corner points [30, 33]. While CCD is particularly suitable for sequential modeling and robust prediction, BBD provides a more cost-effective alternative when operational safety or physical constraints prevent the use of extreme parameter combinations [34–36]. In this study, hydrometallurgical processing of spent dry cell batteries is conducted using microwave-assisted heating combined with H_2O_2 as a reducing agent. Key variables, including extraction time and reductant dosage, are analyzed using a CCD to identify optimal conditions that optimize manganese leaching recovery from spent dry cell waste.

2 Experimental

2.1 Instrumentation

This study was conducted at the Biomass and Energy Laboratory, Faculty of Engineering, Universitas Pembangunan Nasional "Veteran" Jawa Timur, Surabaya, Indonesia. The experimental work and data analysis were carried out from January to June 2025. Materials used in this study include "ABC" dry cell batteries collected from household waste in the city of Surabaya, H_2SO_4 (98%), H_2O_2 (50%), KMnO_4 (99%), and dihydrated oxalic acid ($\text{H}_2\text{C}_2\text{O}_4 \cdot 2\text{H}_2\text{O}$, >98%) all is extra pure for analysis grade supplied by CV (Chemical Indonesia Multi Sentosa, Surabaya). Demineralized water used in this study was obtained from UD (Nirwana Abadi, Surabaya). The instrument used in this study include modified Electrolux Microwave Model EMG23K22B with magnetic stirrer and 40 cm Allihn condenser which

operates power at 240 W and 300 rpm of stirring as shown in Fig. 1. Permanganometric titration and an X-ray fluorescence (NEX QC+, Rigaku, Tokyo, Japan) equipped with QuanTEZ software and a detector of < 160 eV @Mn K-alpha line, were used to determine the MnO₂ composition on solid sample. From the permanganometric analysis (according to ASTM E465-24 [37]) the MnO₂ composition was calculated by Eq. (1).

$$\% \text{MnO}_2 = \frac{\left(\frac{m_{\text{H}_2\text{C}_2\text{O}_4}}{EW_{\text{H}_2\text{C}_2\text{O}_4}} - V_{\text{KMnO}_4} \times N_{\text{KMnO}_4} \right) \times EW_{\text{MnO}_2}}{m_{\text{sample}}} \times 100\% \quad (1)$$

The $m_{\text{H}_2\text{C}_2\text{O}_4}$ is the mass of added oxalic acid (g), $EW_{\text{H}_2\text{C}_2\text{O}_4}$ is the equivalent mass of oxalic acid (g/eq), V_{KMnO_4} is the volume of potassium permanganate titrant used (L), N_{KMnO_4} is the normality of the potassium permanganate solution (eq/L), EW_{MnO_2} is the equivalent mass of manganese dioxide (g/eq), and m_{sample} is the mass of the dry cell sample (g).

2.2 Preparation

The manganese-carbon mixture was recovered by stripping the zinc casing from spent dry cells and washing it with demineralized water until the filtrate reached a neutral pH 7 to ensure the complete removal of residual electrolytes. The resulting black residue was subsequently oven-dried at 110 °C for 1 h and pulverized to a particle size of 150 mesh (99.33 μm) to enhance the surface area for optimal extraction efficiency. The chemical composition of the prepared "ABC" dry cell sample used in this

study was determined by X-ray fluorescence (XRF) and is given in Table 1.

Based on Table 1, the chemical composition can be calculated using Eqs. (2)–(5).

$$m_{\text{MnO}_2} = \frac{m_{\text{Mn}}}{MW_{\text{Mn}}} \times MW_{\text{MnO}_2} \quad (2)$$

$$m_{\text{ZnCl}_2} = \frac{m_{\text{Cl}}}{2 \times MW_{\text{Cl}}} \times MW_{\text{ZnCl}_2} \quad (3)$$

$$m_{\text{ZnO}} = \left(\frac{m_{\text{Zn}}}{MW_{\text{Zn}}} - \frac{m_{\text{Cl}}}{2 \times MW_{\text{Cl}}} \right) \times MW_{\text{ZnO}} \quad (4)$$

$$\% \text{mass}_i = \frac{m_i}{m_{\text{total}}} \times 100\% \quad (5)$$

The m_{Mn} is the mass of manganese (g), m_{Cl} is the mass of chlorine (g), m_{Zn} is the mass of zinc, m_{MnO_2} is the mass of MnO₂ (g), m_{ZnO} is the mass ZnO compound (g), m_{ZnCl_2} is mass of ZnCl₂ (g), MW_{Mn} is the molar mass of Mn, MW_{Cl} is the molar mass of Cl, MW_{Zn} is the molar mass of Zn (g/gmol), MW_{MnO_2} is the molecular mass of MnO₂, MW_{ZnO} is the molecular mass of ZnO, MW_{ZnCl_2} is the molar mass of ZnCl₂, %mass_{*i*} is the mass percentage of compound *i*, m_i is the mass of compound *i*, and m_{total} is the total mass of the sample. The results of the calculations by Eqs. (1)–(5) are shown in Table 2. The spent dry cell contains ZnCl₂ because it works through a reduction–oxidation reaction, one of which is the reaction between zinc and NH₄Cl that converts zinc to ZnCl₂.

2.3 Microwave-assisted leaching

10 g of the prepared sample was dissolved in 100 mL 1.2 M H₂SO₄ with a 0–2% w/v solvent of H₂O₂ and subsequently subjected to microwave-assisted leaching. The process was conducted at a power of 240 W, a stirring speed of 300 rpm, and a temperature of 80 °C for 10–50 min. Following the reaction, the mixture was filtered to isolate the carbon residue. The filtrate was collected for the subsequent precipitation stage to obtain purified MnO₂.

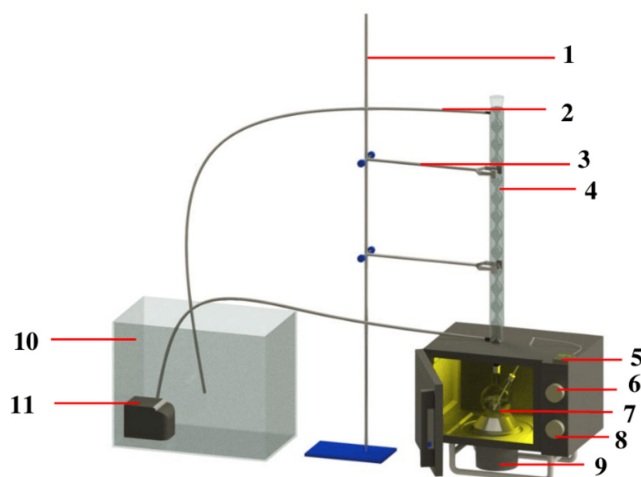


Fig. 1 Microwave-assisted instrumentation. 1. Stand, 2. Hose, 3. Clamp, 4. Condenser, 5. Thermocouple, 6. Power set, 7. 500 mL two neck flat bottom flask, 8. Time set, 9. Magnetic stirrer, 10. Water tank, 11. Water pump

Table 1 XRF analysis of "ABC" dry cell sample

Composition	Mn	Zn	Cl
%mass	58.78	40.46	0.76

Table 2 Chemical composition of prepared the "ABC" dry cell sample

Composition	MnO ₂	ZnO	ZnCl ₂
%mass	64.61	34.37	1.02

2.4 Oxidative precipitation

Precipitation was carried out by adding 0.25 M KMnO_4 until the solution attained a persistent purple coloration, followed by a 20-min reaction period at 25 °C under constant stirring at 300 rpm. Upon filtration, the residue was washed with demineralized water until the filtrate became colorless to ensure the complete removal of excess KMnO_4 . The resulting MnO_2 deposit was subsequently oven-dried at 110 °C for 1 h.

2.5 Optimization model

RSM was employed to model the manganese recovery from the spent dry cells through a hydrometallurgical process, specifically utilizing a CCD to evaluate the interaction and significance of H_2O_2 concentration (*A*) and leaching time (*B*). A face-centered CCD ($\alpha = \pm 1$) comprising 10 experimental runs with two center-point replicates was executed via *Design Expert* Version 13.00 [38] to identify the optimal operational conditions for maximizing the recovery percentage. The response can be represented graphically, either in the three-dimensional space or as contour plots that help visualize the shape of the response surface. The ranges and the levels of the factors investigated in the model are given in Table 3.

3 Result and discussion

3.1 Characterization

The purity of the recovered MnO_2 was analyzed using the ASTM E465-24 [37] permanganometric titration using Eq. (1), followed by X-ray Fluorescence (XRF) analysis to verify the results, with the corresponding recovery data across various H_2O_2 concentrations and leaching times presented in Table 3.

Fig. 2 shows consistently high MnO_2 purity between 95.36–97.74% in several conditions with standard error between 0.72–5.87% based on ASTM E465-24 [37] permanganometric analysis. Based on XRF analysis in Table 4, the chemical compounds composition can calculate using Eqs. (2)–(5).

Table 4 shows that the final precipitate achieved a MnO_2 purity 95.95–97.15%, a substantial increase from the 64.61% found in the raw material as shown in Table 2.

Table 3 Central composite design factors and independent variables

Variable (unit)	Factor	Levels		
		–	0	+
H_2O_2 (%w/v)	<i>A</i>	0	1	2
Time (min)	<i>B</i>	10	30	50

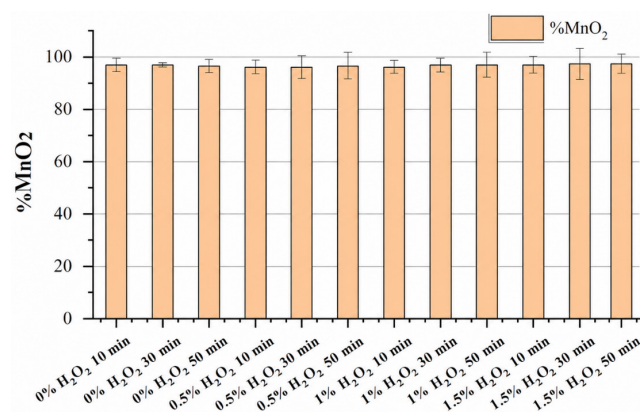


Fig. 2 Purity of MnO_2 based on ASTM E465-24 [37] permanganometric analysis

This enhancement demonstrates that the hydrometallurgical process using 1.2 M H_2SO_4 , H_2O_2 as a reductant, microwave-assisted leaching and oxidative precipitation can effectively eliminate major impurities. Specifically, ZnO levels (in ZnSO_4 form) dropped from 34.37% to 2.50–3.66%, while ZnCl_2 decreased from 1.02% to 0.21–0.59%.

The process efficiency is attributed to the use of KMnO_4 as a precipitator, which selectively reacts with dissolved manganese to form MnO_2 deposits. In the study by Peng et al. [39], the selection of extraction parameters was carefully justified from both chemical and thermodynamic perspectives. The use of 1.2 M H_2SO_4 was chosen based on stoichiometric considerations to provide optimal H^+ activity capable of fully dissolving the zinc and manganese oxides from the complex dry cell matrix. Using a lower concentration could lead to incomplete dissolution due to acid depletion during the reaction. Conversely, utilizing a higher concentration would result in an excessive amount of unreacted free acid in the system, which not only increases the consumption of neutralizing agents in the subsequent precipitation stage but also risks equipment corrosion under microwave irradiation [39].

Furthermore, the solid-to-liquid ratio (mass of solid material to the volume of solution) was selected to ensure the optimal mass transfer and uniform heating. A highly concentrated slurry increases viscosity, leading to uneven microwave energy distribution (hotspots) and poor leaching kinetics, whereas a highly dilute solution decreases the economic viability of the process. Finally, the choice of H_2O_2 concentration within the 0–2% (w/v) range is justified by its stability under microwave heating. While H_2O_2 is an excellent reducing agent for converting insoluble Mn^{4+} to soluble Mn^{2+} , concentrations exceeding 2% under intense microwave irradiation rapidly undergo auto-decomposition into

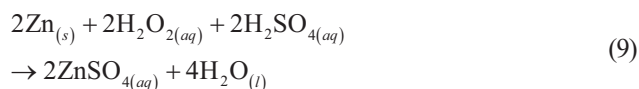
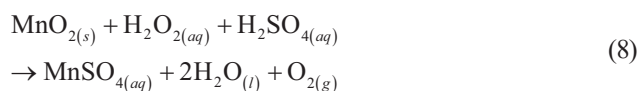
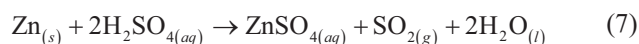
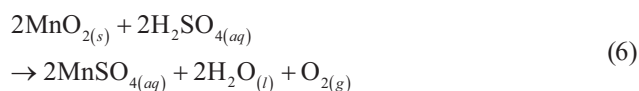
Table 4 Chemical composition based on XRF analysis

Factor		Elements			Compounds		
H ₂ O ₂ (%w/v)	Time (min)	Mn	Zn	Cl	MnO ₂	ZnSO ₄	ZnCl ₂
0	10	97.67	2.02	0.32	96.95	2.66	0.39
	30	97.76	1.92	0.32	97.10	2.51	0.39
	50	97.35	2.29	0.36	96.54	3.02	0.44
0.5	10	97.01	2.67	0.32	95.95	3.66	0.39
	30	96.91	2.59	0.50	96.10	3.30	0.60
	50	97.53	2.27	0.20	96.54	3.22	0.24
1	10	97.23	2.51	0.26	96.18	3.51	0.31
	30	97.38	2.30	0.32	96.51	3.11	0.38
	50	97.76	2.03	0.21	96.91	2.84	0.25
1.5	10	97.77	1.93	0.30	97.08	2.56	0.36
	30	97.71	2.05	0.25	96.89	2.81	0.30
	50	97.87	1.95	0.18	97.03	2.75	0.22
2	10	97.83	1.88	0.29	97.15	2.50	0.35
	30	97.61	2.08	0.31	96.85	2.77	0.38
	50	97.47	2.26	0.27	96.57	3.11	0.32

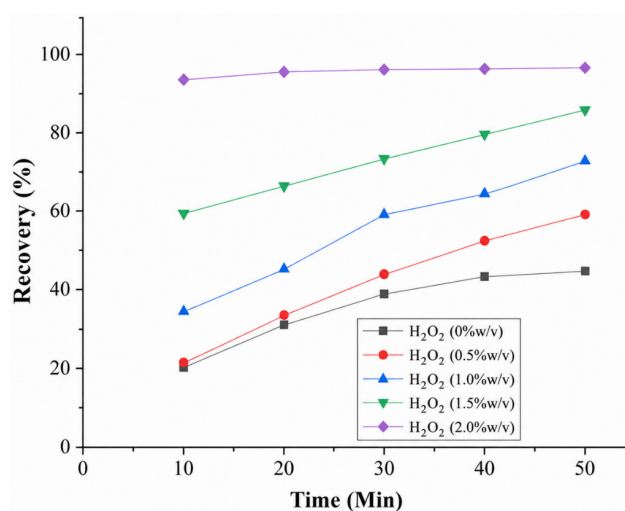
water and oxygen gas due to thermal effects. This excessive decomposition would waste the reductant and generate significant gas pressure, compromising both efficiency and safety. Van Benschoten et al. [40] and Freitas et al. [41] report high Mn recovery rates (>99,5%) through similar oxidative precipitation methods. Consequently, the high purity achieved within the tested parameters confirms the stability and operational effectiveness of this recovery process. Residual ZnSO₄ and NH₄Cl impurities persist in the final product due to the porous morphology of MnO₂ that facilitates the diffusion and subsequent entrapment of Zn²⁺ and Cl⁻ ions within the internal pore structure of the manganese dioxide precipitate [42, 43].

3.2 Effect of reductant addition and time

Manganese leaching via microwave irradiation reduces Mn⁴⁺ to soluble Mn²⁺ in H₂SO₄ to produce MnSO₄. While the process occurs independently, reductants like H₂O₂ significantly optimize the efficiency, achieving recovery rates as high as 99.04% in manganese ore leaching [25, 27, 28]. Microwave energy accelerates this redox reaction by enhancing molecular collisions and ionic mobility, which destabilizes Mn–O bonds in the MnO₆ octahedral framework. Compared to conventional heating, microwave-assisted methods offer a 20% increase in efficiency [25]. The resulting Mn²⁺ is subsequently converted into high-purity MnO₂ through KMnO₄ precipitation. Reaction mechanism in leaching process is shown in Eqs. (6) and (7) without H₂O₂ as reductant, in Eqs. (8) and (9) with H₂O₂ reductant [44, 45].



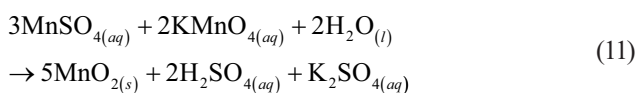
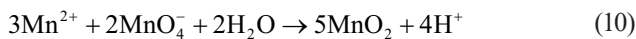
The influence of H₂O₂ concentration on MnO₂ recovery, as illustrated in Fig. 3, demonstrates that the

**Fig. 3** The effect of reductant concentration on recovery efficiency

recovery efficiency is highly dependent on the presence of a reducing agent to convert inert Mn^{4+} into soluble Mn^{2+} [46]. Without H_2O_2 , the recovery remained below 40%, whereas the addition of 0.5–1% w/v H_2O_2 significantly enhanced the recovery to approximately 88% by providing active peroxide species that lower the activation energy of the reduction process [11]. The optimum recovery of approximately 96% was achieved at 2% w/v H_2O_2 within 20–50 min, representing a stoichiometric balance between the reductant and the metal oxide. However, increasing the concentration beyond 2% w/v resulted in decreased efficiency due to the rapid thermal decomposition of H_2O_2 into O_2 under microwave irradiation and the potential back-oxidation of Mn^{2+} ions [47]. The kinetic profiles indicate a rapid initial leaching phase in the first 10 min followed by stabilization, confirming that the combination of microwave activation and 2% w/v H_2O_2 provides the most effective conditions for maximizing MnO_2 recovery from spent dry cell batteries [27].

3.3 MnO_2 precipitation

To accurately determine the true recovery of manganese from the spent dry cells, a rigorous mass balance was applied during the precipitation stage. Oxidative precipitation using $KMnO_4$ was selected because it has high selectivity and provides a high recovery yield up to 99.9% [41]. The reaction mechanism in precipitation process is shown in Eqs. (10) and (11) [44, 45].



Based on Eqs. (8) and (11), the amount of leached MnO_2 from dry cell and MnO_2 recovery can be calculated using Eqs. (12)–(14).

$$m_{MnO_2, final} = \%_{MnO_2} \times m_{precipitate} \quad (12)$$

$$m_{MnO_2, leached} = \frac{3}{5} \times m_{MnO_2, final} \quad (13)$$

$$Recovery = \frac{m_{MnO_2, leached}}{m_{MnO_2, dry\ cell}} \times 100\% \quad (14)$$

The $m_{precipitate}$ is the mass of the precipitate (g), $m_{MnO_2, leached}$ is the mass of MnO_2 leached from the dry cell (g), $m_{MnO_2, final}$ is the mass of MnO_2 precipitated (g), $m_{MnO_2, dry\ cell}$ is the mass of MnO_2 in the dry cell (g) and $\%_{MnO_2}$ is the purity of MnO_2 in the precipitate (%). Results of the calculations from Eqs. (12)–(14) are shown in Fig. 3.

The final MnO_2 precipitate originates from two distinct sources: the dissolved Mn^{2+} extracted from the dry cell waste, and the reduction of the $KMnO_4$ reagent itself. Based on the stoichiometric ratio, exactly 2 mol $KMnO_4$ are consumed to precipitate 3 mol of dissolved Mn^{2+} , resulting in 5 mol of MnO_2 . From the precise titration volume of 0.25 M $KMnO_4$ required to completely precipitate the dissolved Mn, the mass of manganese originating from the permanganate was explicitly calculated (Table 5). To eliminate any positive bias, this reagent-derived manganese mass was subtracted from the total mass of the final precipitate. Consequently, the reported recovery percentages strictly reflect the true mass of manganese successfully extracted and recovered solely from the battery waste matrix.

Otherwise, there are some processes for MnO_2 precipitation. Table 6 shows that the permanganate oxidative precipitation provides the highest recovery (99.5–99.9%) but involves strong oxidants and higher costs [40, 41]. Electrolysis offers a cleaner process (93%) but requires high energy and expensive electrodes [48].

Table 5 Amount of $KMnO_4$ precipitator and MnO_2 precipitate

Factor	Time (min)	Volume of 0.25 M $KMnO_4$ (mL)	m precipitate (g)
0	10	43.0	2.25
	20	65.3	3.48
	30	80.6	4.32
	40	89.1	4.79
	50	92.6	4.98
0.5	10	46.1	2.42
	20	71.1	3.80
	30	91.5	4.92
	40	108.0	5.83
	50	122.0	6.60
1	10	72.4	3.87
	20	94.2	5.07
	30	122.0	6.60
	40	134.2	7.27
	50	149.4	8.11
1.5	10	121.1	6.55
	20	134.3	7.28
	30	148.7	8.07
	40	160.0	8.69
	50	173.6	9.44
2	10	190.8	10.39
	20	193.9	10.56
	30	196.6	10.71
	40	195.9	10.67
	50	198.1	10.79

Table 6 MnO₂ precipitation process

Process	Material	Recovery (%)	Reference
Permanganate oxidative precipitation	KMnO ₄	99.5–99.9	[40, 41]
Electrolysis	Ti/IrO ₂	93	[48]
Oxalate precipitation (calcination precursor)	H ₂ C ₂ O ₄ (Oxalic acid)	96	[49]
Carbonate precipitation	Na ₂ CO ₃	93.4	[50]
	(NH ₄) ₂ CO ₃	90.8	[51]
Persulfate oxidative precipitation	(NH ₄) ₂ S ₂ O ₈	95.5	[52]

Oxalate precipitation (96%) works under milder conditions but needs additional calcination and handling of organic reagents [49]. Carbonate methods (90.8–93.4%) are simpler and cheaper, though with lower recovery and needs additional calcination [50, 51]. Persulfate oxidation (95.5%) gives good efficiency but may increase cost and introduce sulfate residues [52].

3.4 Optimization

A total of 10 runs were calculated following the face centered central composite design protocol as shown in Table 7. The hydrometallurgical process to recover MnO₂ was executed according to each designated set point. Table 7 also presents the experimental and predicted glucose response values for comparison.

The linear model was identified as the most suitable fit due to its superior value on adjusted R^2 (0.8908) and predicted R^2 (0.8071), coupled with a lower sequential p -value (0.0002) and a high lack of fit p -value (0.1952). Consequently, this model was selected for the ANOVA modeling presented in Table 8. A smaller p -value ($p < 0.05$)

Table 7 RSM design experimental and predicted value

Run	Factor A: H ₂ O ₂ (%w/v)	Factor B: Time (min)	Response Y: Recovery (%)	
			Experimental	Predicted
1	1	30	59.15	61.27
2	0	30	38.95	30.77
3	2	30	96.32	91.76
4	1	30	55.57	61.27
5	1	50	72.70	72.19
6	0	50	44.64	41.70
7	1	10	34.57	50.34
8	0	10	20.26	19.85
9	2	50	96.76	102.69
10	2	10	93.74	80.84

indicates a higher probability of significant variable validity. While R^2 determines the relationship between response and independent variables, the adjusted R^2 reflects the actual variability within the equation regarding data distribution; therefore, both values should ideally approach 1.0 [53].

Based on Table 8, the experimental data were fitted to a linear polynomial model represented by Eq. (15).

$$Y = 14.3851 + 30.49362 \times A + 0.546262 \times B \quad (15)$$

The Y denotes the recovery rate (%) and variables A (reductant dosage) and B (time) serve as independent factors. ANOVA results confirm the model's high statistical significance, evidenced by an F -value of 37.72 and a mere 0.02% probability of noise interference. While both factors are significant ($p < 0.05$), factor A exhibits a higher level of significance than B . The model's adequacy is further validated by a non-significant lack of fit ($F = 14.98$, $p = 0.1952$), an R^2 of 0.9151, and a close agreement between adjusted and predicted R^2 (difference < 0.2). Finally, an adequate precision of 16.5559 confirms a robust signal-to-noise ratio, exceeding the required threshold of 4 [54].

The strong correlation between the predicted and actual values, as illustrated in Fig. 4, underscores the reliability and accuracy of the model in forecasting manganese recovery during the leaching process. This visual representation confirms that the model consistently captures the relationship between simulation results and experimental data across various time frames and reductant types. In the plot of predicted versus experimental results, the close proximity of data points to the linear regression line indicates an excellent model fit. Consequently, the alignment of these data points suggests that the mathematical model effectively accounts for the impact of reaction time and reductant dosage on manganese recovery within the hydrometallurgical process [55].

Fig. 5 presents the contour and three-dimensional response surface plots, illustrating the interactive effects of H₂O₂ dosage (A) and reaction time (B) on manganese recovery during the microwave-assisted hydrometallurgical leaching. The color spectrum within these plots serves as a qualitative measure of recovery efficiency: warmer tones transitioning toward red denote higher response values, while cooler shades, such as blue and green, signify reduced yields [56]. These color variations highlight the significant influence of H₂O₂ as a reductant on the dissolution of manganese dioxide, with the maximum recovery localized in the red regions of the plots. Consequently,

Table 8 ANOVA results for the predictive modeling of recovery in hydrometallurgical processing

Source	Sum of squares	df	Mean square	F-value	p-value	
Model	6295.33	2	3147.66	37.72	0.0002	Significant
A: H ₂ O ₂	5579.17	1	5579.17	66.86	<0.0001	
B: Time	716.16	1	716.16	8.58	0.0220	
Residual	584.15	7	83.45			
Lack of fit	577.73	6	96.29	14.98	0.1952	not significant
Pure error	6.43	1	6.43			
Corrected total	6879.48	9				
Fit statistics						
Std. Dev.	9.14		R ²	0.9151		
Mean	61.27		Adjusted R ²	0.8908		
C.V. %	14.91		Predicted R ²	0.8071		
			Adequate precision	16.5559		

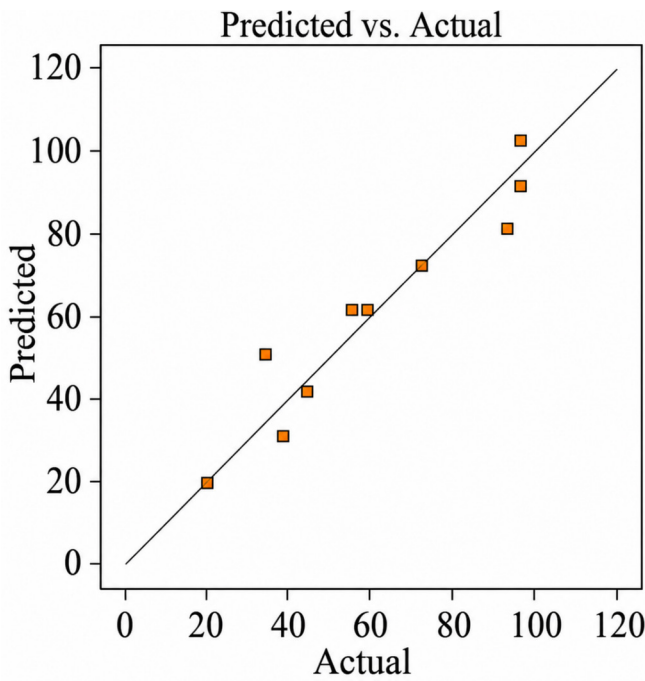


Fig. 4 Predicted vs. actual plot for the recovery of MnO₂

it can be observed that a synergistic increase in both the H₂O₂ concentration and reaction time leads to a substantial enhancement in the manganese recovery.

Utilizing the derived regression model based on Eq. (15), the predicted optimum yield was determined to be 96.8% under an H₂O₂ dosage 2% w/v and a duration 39.15 min (Table 9). Desirability was employed as a metric to evaluate the alignment of the optimal solution with the targeted responses, where a value of 1 signifies a perfect scenario [57]. A desirability score exceeding 0.8 is generally required for robust process optimization [54]. These findings demonstrate that both H₂O₂ concentration and reaction time exert significant, interrelated influences on the manganese recovery rate, with the peak of the response

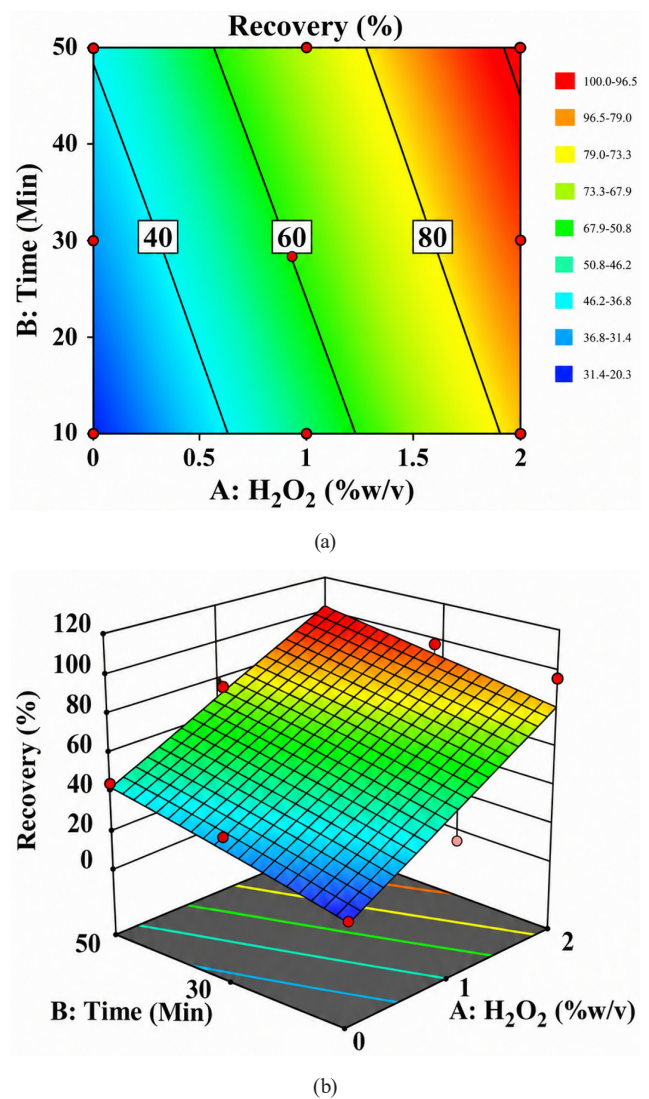


Fig. 5 (a) Contour plot and (b) 3D response surface plot illustrating the interaction between factor A and B on manganese recovery

surface plot identifying the ideal conditions for maximizing process efficiency.

Table 9 Numerical optimization results

Name	Goal	Lower limit	Upper limit	Lower weight	Upper weight
A: H ₂ O ₂	is in range	0	2	1	1
B: Time	Minimize	10	50	1	1
Recovery	Maximize	90	96.7608	1	1
A: H ₂ O ₂ (%w/v)	B: Time (min)	Recovery (%)	Composite desirability		
2	39.154	96.761	0.805		

4 Conclusion

While metallic impurities such as zinc are readily soluble in dilute acids, extracting manganese from spent dry cell batteries is highly challenging due to the chemical stability and insolubility of MnO₂. This study demonstrates that overcoming this barrier necessitates a synergistic approach using microwave-assisted heating and H₂O₂ as a reducing agent. The reductant is strictly required to convert the inert Mn⁴⁺ into soluble Mn²⁺, while the microwave energy drastically accelerates the reaction kinetics. The permanganate oxidative precipitation is the simplest process and most efficient method with the highest recovery, but it comes with higher cost and handling complexity. Other methods such as electrolysis, oxalate, carbonate and persulfate precipitation offer more practical or economical alternatives, though generally with slightly lower recovery. Optimization via RSM and CCD identified the ideal conditions as 2% w/v H₂O₂ and a leaching time of 39.15 min, resulting in a verified MnO₂ recovery of 96.8%. The recovered product achieved a high

MnO₂ purity of 96–97%, surpassing the standard commercial electrolytic manganese dioxide (EMD) threshold > 92%.

In contribution to the state of the art, this study proves that the integration of microwave irradiation and chemical reduction accelerates the processing time to under 40 min, offering a significant advantage over conventional methods. This integrated approach not only provides a highly time- and energy-efficient pathway for valorizing hazardous spent dry cell batteries but also offers a viable technical framework for scaling up secondary manganese resource recovery. Consequently, future research should explore variables, such as acid concentration range, solid-to-liquid ratios and microwave power levels, to further refine the purity and gain a comprehensive understanding of the process kinetics.

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